## Chapter <br>  <br> Unit Pricing and Currency Exchange




## REVIEW: WORKING WITH FRACTIONS

In this section, you will use fractions to solve for unknown values.

## Example 1

Simplify $\frac{18}{27}$.

## SOLUTION

factor: one of two or more numbers that, when multiplied together, form a product. For example, 2 .
3 , and 6 are factors of the product 6 because:
$1 \times 6=6$
$2 \times 3=6$
$3 \times 2=6$
$6 \times 1=6$

The fractions $\frac{18}{27}$, $\frac{6}{9}$, and $\frac{2}{3}$ are equivalent fractions because they
represent the same amount.

To simplify a fraction, state the fraction in its lowest terms. To find the lowest terms, divide the numerator and the denominator by their largest common factor.

$$
\begin{aligned}
& \frac{18}{27} \leftarrow \text { numerator } \\
& \leftarrow \text { denominator }
\end{aligned}
$$

Identify the factors of 18 and 27.


The largest factor common to both 18 and 27 is 9 . Divide both the numerator and the denominator 159 .

$$
\begin{aligned}
& \frac{18}{27}=\frac{18 \div 9}{27 \div 9} \\
& \div 9 \\
& \div 9
\end{aligned}=\frac{2}{3}
$$

$$
\frac{18}{27}=\frac{2}{3}
$$

## ALTERNATIVE SOLUTION

Using the largest common factor when simplifying fractions takes the least number of steps, but you can use any common factor.

$$
\begin{aligned}
\frac{18}{27} & =\frac{18 \div 3}{27 \div 3} \\
\frac{18 \div 3}{27 \div 3} & =\frac{6}{9} \\
\frac{18}{27} & =\frac{6}{9} \\
\frac{6}{9} & =\frac{6 \div 3}{9 \div 3} \\
\frac{6 \div 3}{9 \div 3} & =\frac{2}{3} \\
\frac{6}{9} & =\frac{2}{3}
\end{aligned}
$$



Simplify further, again using the factor 3.

## BUILD YOUR SKILLS

1. Simplify these fractions to their lowest terms.
a) $\frac{4}{16}=$
b) $\frac{3}{12}=$
c) $\frac{25}{75}=$
e) $\frac{8}{18}=$
f) $\frac{45}{100}=$

h) $\frac{3}{21}=$
i) $\frac{7}{56}=$
g) $\frac{20}{50}=$

## Example 2

Solve for $x$ in this equation containing fractions.
$\frac{x}{16}=\frac{5}{24}$

## SOLUTION

To solve an equation, the same operation must be applied to both sides of the equation.

Begin by multiplying both sides of the equation by the same number so that you can clear it of fractions (by eliminating the denominators). This will allow you to isolate $x$.
multiple: the product of a number and any other number. For example,
2, 4, 6, and dare some multiples of 2 because:
$2 \times 1=2$
The simplest multiplier is the lowest common denominator of the two fractions. Identify the multiples of 16 and 24.
$2 \times 2=4$
$2 \times 3=6$
$16=\{16,32,48,64,80, \ldots\}$
$2 \times 4=8$
$24=\{24,48,72,96, \ldots\}$

The lowest common multiple between 16 and 24 is 48 , so begin solving the equation by multiplying both fractions by 48 .

$$
\frac{x}{16}=\frac{5}{24}
$$

$48 \times \frac{x}{16}=\frac{5}{24} \times 48 \quad$ Multiply by 48.

$$
\frac{48 x}{16}=\frac{240}{24} \quad \text { Simplify }
$$

$$
3 x=10
$$

人 $\frac{3 x}{3}=\frac{10}{3}$ Divide by 3 to isolate $x$.

If $x$ is not a whole number, it is best to leave the answer as a fraction or in mixed numeral form rather than as a decimal
because the decimal answer would often
have to be rounded.

$$
\frac{x}{16}=\frac{5}{24}
$$

$(24 \times 16) \times \frac{x}{16}=\frac{5}{24} \times(16 \times 24)$

$$
\begin{aligned}
384 \times \frac{x}{16} & =\frac{5}{24} \times \\
\frac{384 x}{16} & =\frac{1920}{24}
\end{aligned}
$$

$$
24 x=80
$$

$$
\frac{24 x}{24}=\frac{80}{24}
$$

$$
x=\frac{80}{24}
$$

$$
x=\frac{80 \div 8}{24 \div 8}
$$

$$
x=\frac{10}{3} \text { or } 3 \frac{1}{3} \text { or } 3 . \overline{3}
$$

Simplify.

Divide both sides by 24 to isolate $x$.

Simplify, using the factor 8 .

## BUILD YOUR SKILLS

2. Solve for $x$.
a) $\frac{x}{10}=\frac{40}{50}$
b) $\frac{12}{16}=\frac{18}{x}$
有/大/
c) $\frac{56}{64}=\frac{x}{8}$
chs
d) $\frac{18}{27}=\frac{36}{x}$
e) $\frac{x}{2056}=\frac{3}{4}$
g) $\frac{3}{5}=\frac{x}{460}$
h) $\frac{25}{x}=\frac{40}{200}$

ratio: a comparison between two numbers measured in the same units

## NEW SKILLS: WORKING WITH RATIO AND PROPORTION

When a carpenter bonds two pieces of wood with epoxy resin, she must first mix the epoxy with a hardener. She mixes these materials in a ratio of 10 to 1 , where there are 10 parts of epoxy to 1 part of hardener. This ratio can be written as $10: 1$ or as a fraction, $\frac{10}{1}$.

If the carpenter wanted to use 150 parts of epoxy, she would need 15 parts of hardener. This would give her a ratio of 150 to 15 between the amount of epoxy and the amount of hardener. You can write this as 150:15 or as $\frac{150}{15}$.
The ratio $\frac{150}{15}$ can be simplified to $\frac{10}{1}$.


It is common to express ratios as reactions when doing calculations.
proportion: a fractional statement of equality between two ratios

$$
\frac{150}{15}=\frac{10}{1}
$$

For more information, see page 12 of MathWorks 10.
When you state that two ratios are equal, as they are in the following equation, you have written a proportion.

## Example 3

Charles works as a cook in a restaurant. His chicken soup recipe contains:

- 11 cups of seasoned broth
- 5 cups of diced vegetables
- 3 cups of rice
- 3 cups of chopped chicken

He wants to make the recipe at home for his parents. To reduce the recipe yield, he needs to know what the are between the quantities of ingredients.
a) What is the ratio of vegetables to chicken?
b) What is the ratio of broth

c) What is the ratio of chicken to rice?
d) What is the ratio of the chicken to the to pl ingredients in the recipe?

## SOLUTION

a) Since there are 5 cups of vegetables and 3 cups of chief en, the ratio of vegetables to chicken is $5: 3$ or $\frac{5}{3}$.


## A ratio can have

 a numerator larger than the denominator.Because a ratio
compares two numbers, do not rewrite it as a mixed fraction.
b) Since there are 11 cups of broth and 5 cups of vegetables, the ratio of broth to vegetables is $11: 5$ or $\frac{11}{5}$.
c) There are 3 cups of chicken and 3 cups of rice, so the ratio of chicken rouge is $3: 3$ or $\frac{3}{3}$. This can be simplified to $1: 1$ or $\frac{1}{1}$.
d) There are 3 cups of chicken in the recipe, and a total of 22 cups of ingredients. The ratio of chicken to the total amount of ingredients is $3: 22$ or $\frac{3}{22}$.

Although $\frac{1}{1}$ is usually written as the number 1, keep it as a fraction when it

## BUILD YOUR SKILLS

3. For a silk screening project, Jan mixes a shade of orange ink. She uses a ratio of red ink to yellow ink of $2: 3$ and yellow ink to white ink of $3: 1$.
a) How many mL of yellow ink would she need if she used 500 mL of white ink?

4. On a bicycle with more than one gear, the ratio between the number of teeth on the front gear and the number of teeth on the back gear determines how easy it is to pedal. If the front gear has 30 teeth and the back gear has 10 teeth, what is the ratio of front teeth to back teeth?

5. Some conveyor belts have two pulleys. If one pulley has a diameter of 45 cm and another has a diameter of 20 cm , what is the ratio of the smaller diameter to the
larger diameter?
6. Bank tellers use ratios when converting currencies. If $\$ 1.00$ CAD equals approximately
1.13 Australian dollars, what is the ratio of Canadian dollars to Australian dollars?
7. What is the ratio of 250 mL of grape juice concentrate to 1 L of water? (Hint: Converfogh measurements to the same units. There are 1000 mL in 1 L .)

C
8. A mechanic mixes oil with gasto lubricate the cylinders in a motorcycle engine. He uses 1 part oil and 32 parts gat What is the ratio of oil to gas?

## Example 4



Tom and Susan make $\$ 180.00$ from holding a garage sale. Because Tom contributed fewer items to the sale, the money is to be divided between Tom and Susan in the ratio of $1: 2$. How much money will each person receive?

## SOLUTION

Since the ratio is $1: 2$, this means that for every $\$ 1.00$ Tom receives, Susan receives $\$ 2.00$. Stated another way, this means that for every $\$ 3.00$ earned, Tom get $\$ 1.00$ and Susan gets $\$ 2.00$.

Therefore, Tom receives $\frac{1}{3}$ of the money and Susan receives $\frac{2}{3}$ of it.


## BUILD YOUR SKILLS

9. The ratio of flour to shortening in a recipe for piecrust is $2: 1$. If a baker makes 30 cups of piecrust, how many cups of flour and shortening does he use?


0
10. A compound of two chemicals is mixed in the ratio of $3: 10$. If there are 45 litres of the compound how much of each chemical is in the mixture?
11. Cheryl is an automotive repair technician. She unixes paint and thinner to apply to a bus. The instructions say to mix paint with thinner in the ratio of 5:3. If Cheryl needs 24 L of paint/thinner mixture, how much of each will she use?


## NEW SKILLS: WORKING WITH RATE

A rate is a ratio comparing two numbers measured in different units.
Some examples of rates are:

- $\$ 1.69 / 100 \mathrm{~g}$ or $\frac{\$ 1.69}{100 \mathrm{~g}}$ for the cost of ham at the deli
rate: a comparison between two numbers measured with different units
- $80 \mathrm{~km} / \mathrm{h}$ or $\frac{80 \mathrm{~km}}{1 \mathrm{~h}}$ for how fast a car travels
- $\$ 38.0074$ hor $\frac{\$ 38.00}{4 \mathrm{~h}}$ for how much you earn at work

For more information, see page 17 of MathWorks 10.

## Example 5

The amount of fuel consumed vehicle when it is driven 100 km is referred to as the rate of fuel consumption. Write a rate statement that indicates that a car uses 6.3 litres of gas for every 100 km driven.

SOLUTION
$6.3 \mathrm{~L}: 100 \mathrm{~km}, \frac{6.3 \mathrm{~L}}{100 \mathrm{~km}}$, or $6.3 \mathrm{~L} / 100 \mathrm{~km}$


## BUILD YOUR SKILLS

12. Write a rate statement that indicates that you earned $\$ 65.00$ interest onyour investment in the last 3 months.
13. Write a rate statement that indicates how much you earn in an 8 -hour day if you are paid $\$ 9.25$ for each hour you work.
14. Write a rate statement that indicates that 1 cm on a map represents 2500 km in real distance.

## Example 6

If you earn $\$ 150.00$ in 12 hours, how much will you earn if you work 40 hours?

SOLUTION

16. As a janitor, Janine makes a cleaning solution by mixing 30 g of concentrated powdered cleanser into 2 L of water. How much powder will she need for 5 L of water?

17. An office has decided rack how much paper it uses to reduce waste. At the end of each month, the secretary cords the total number of sheets used and their mass. If paper has a mass of 4.9 kg forever 500 sheets, what is the mass of 700 sheets of paper?

## PRACTISE YOUR NEW SKILLS

1. Find the unknown value in each of the following proportions. Give answers to the nearest tenth of a unit (to one decimal place).
a) $\frac{24}{18}=\frac{x}{12}$
b) $\frac{168 \mathrm{~km}}{2 \mathrm{~h}}=\frac{548 \mathrm{~km}}{x \mathrm{~h}}$
c) $\frac{40}{28}=\frac{60}{x}$
d) $\frac{6 \text { pizza slices }}{2 \text { people }}=\frac{x \text { pizza slices }}{21 \text { people }}$
g) $\frac{7}{15}=\frac{x}{1}$
f) $\frac{12}{25}=\frac{25}{x}$
8) $\frac{8 \text { bundles }}{}=\frac{24 \text { bundles }}{8}$
$25 x$

些
h) $\frac{12}{45}=\frac{16}{x}$


2. A hairdresser mixes brunette hair colouring for a client using 20 nt hair colour, 40 mL colour developer, 15 mL conditioner, and 3 mL thickener. Find he following ratios and simplify them to their lowest terms. Express your answers as fractions.
a) The ratio of hair colour to thickener.
b) The ratio of thickener to conditioner.
c) The ratio of colour developer to hair colour.


d) If this treatment costs the customer $\$ 68.00$ and the cost of labour and materials used is $\$ 14.20$, what is the ratio customer price to actual cost?

3. If the ratio of yellow pigment to blue pigment in a shade of green pain is $2: 3$, how many drops of yellow pigment will be needed if 12 drops of blue are used?
4. If 5 cm on a map represents 2.5 km of actual ground, how many centimetres would 15 km of actual ground be on the map?

5. If a cal paint will cover $48 \mathrm{~m}^{2}$ of wall space, how many cans will you need to paint 220 mf?


6. The ratio of teeth on a pair of driving gears is $13: 6$, With the larger gear having more teeth. If the larger gear has 52 teeth, how many does the smaller gear have?

7. If Stephie can type 75 words per minute, how long will it take her to type an 800 -word term paper? Is the solution a rate or a ratio? Explain your answer.
8. If the ratio of flour to sugar in a recipe is $3: 2$, how much flour would you need if you used 1.5 cups of sugar?


## Unit Price

## NEW SKILLS: WORKING WITH UNIT PRICE

unit price: the cost of one unit; a rate expressed as a fraction in which the denominator is 1

When items are sold in quantities of more than 1 , the unit price indicates how much 1 of the items would cost. For example, if you buy a package of 3 pencils, the unit price is the price of 1 pencil.

Fol more information, see page 23 of MathWorks 10.

## Example 1

If a carton on d dozen eggs costs $\$ 3.29$, how much are you paying for 1 egg?

## SOLUTION

Solve using a proportion. Let $x$ represent the cost of 1 egg.

$$
\begin{aligned}
\frac{\$ 3.29}{12 e g g s} & =\frac{x}{1 \operatorname{egg}} \\
\frac{3.29}{12} & =\frac{x}{1} \\
12 \times \frac{3.29}{12} & =\frac{x}{1} \times 12 \\
3.29 & =12 x \\
\frac{3.29}{12} & =\frac{12 x}{12} \\
\frac{3.29}{12} & =x \\
0.27 & \approx x
\end{aligned}
$$



Omit the units in the calculation.


Multiply both sides of the equation by 12 Simplify.


Divide both sides by 12 to jo


One egg costs approximately $\$ 0.27$.

## BUILD YOUR SKILLS

1. If 12 apples cost $\$ 10.20$, how much does one apple cost?

2. Lindsay is the kitchen manager of an Ethiopian café. She purchases a case of 1000 paper coffee cups for $\$ 94.83$. How much does one cup cost?

3. Frank is a locksmith who owns his own business. He buys a case of 144 bulk brass padlocks for $\$ 244.97$. He sells each lock for $\$ 5.50$.
a) How much does each lock cost Frank?
b) How much profit does Frank make when he sells one lock?


People often think
that larger-sized
packages cost less
per unit, but this is
not always so.

## Example 2

Often unit price is used to compare costs.
A $48-$ oz can of tomatoes costs $\$ 2.99$. An 18 -oz can costs $\$ 1.19$. Which is a better buy?

## SOLUTION

Calculate the cost of 1 oz of tomatoes for each size of can.
Calculate the cost of 1 oz from the 48 -oz can.
$2.99 \div 48 \approx \$ 0.062 \quad$ Divide the total cost by the total number of ounces.
1 of of tomatoes costs approximately $\$ 0.06$.
Calculate 1 cost of 1 oz from the $18-\mathrm{oz}$ can.
$\$ 1.19 \div 18 \approx \$ 0.066 \quad$ Divide the total cost by the total number of ounces.
1 oz of tomatoes costo qpproximately $\$ 0.07$.
It costs more for one ounce of tomatoes from the $18-\mathrm{oz}$ can, so the $48-\mathrm{oz}$ can is the better buy.


## BUILD YOUR SKILLS

4. La Boutique du Livre is a francophone bookstore in St. Boniface, MB. It sells notebooks in packages of 12 for $\$ 15.48$. Another bookstore sells the same notebooks in packages of 15 for $\$ 19.65$. Which is the better price?

5. Which is the better buy: 6 muffins for
$\$ 7.59$, or one dozen muffins for $\$ 14.99$ ?
6. Johnny can buy two 8 -foot pieces of $2^{\prime \prime}$ by $4^{\prime \prime}$ lumber at $\$ 2.60$ each, or three 6 -foo pieces for $\$ 1.92$ each. Which is the better buy per foot?

## Example 3

Shirin is the manager of a fabric store and is training a new employee. Shirin wants to make an easy reference chart that lists the prices of different lengths of a fabric. One metre of the fabric costs $\$ 8.42$. Fill in the rest of the chart.


FABRIC COST BY LENGTH

| Length of fabric | Cost of fabric |
| :--- | :--- |
| 0.5 m | $\$ 4.21$ |
| 1 m | $\$ 8.42$ |
| 1.75 m | $\$ 14.74$ |

## alternative solution

You can use unit rates rather than proportions.
1 m costs $\$ 8.42$. Use this unit cost to calculate the cost of the other lengths
$\$ 8.42 \times 0.5=\$ 4.21$
$\$ 8.52 \times 1.75=\$ 14.74$

## BUILD YOUR SKILLS

7. Sasha is a landscape gardener. He sees that a 200-foot roll of string trimmer line costs $\$ 18.75$. A 150 -foot toll of line costs $\$ 15.21$.
a) Which roll of line is the least expensive per foot?
b) What is the difference in price, per foot?
8. If $2 \frac{1}{2} \mathrm{~kg}$ of tomatoes cost $\$ 8.25$, how much will you pay for 7 kg ?

9. If Wayne bought 5 litres of gas for his lawnmower for $\$ 5.45$, how much would he have to pay to fill his car with 48 litres of gas?

## PRACTISE YOUR NEW SKILLS

1. During the summer, Dean works as a cashier in a store near Saskatchewan's Greenwater Lake Provincial Park. The store sells a case of 12 bottles of water for $\$ 8.50$ and individual bottles of the same brand of water for $\$ 1.55$.
a) Approximately how much does each bottle of water in the case of 12 cost?

How mach
b) How machyould a customer save by buying a case of water, rather than 12 individual bottles?

2. Maureen purchased enough carpet to cover rectangular room measuring 7 metres by 12 metres. The carpet costs $\$ 8.15$ per square metre.
a) How much carpet did Maureen buy?

b) How much did the carpet cost?
3. Tyler is a self-employed sheet metal worker. He purchases 25 sheets of aluminum that measure 4 feet by 8 feet. The cost is $\$ 4000.00$ before tax and shipping.
a) How much does 1 sheet cost?
b) What is the price per square foot?

4. A painting business buys 3 -inch wide paintbrushes from a supplier in cases of 6 . One case costs $\$ 31.29$.
a) How much do two brushes cost?

○


b) If a customer buys two or more cases, the supplier reduces the price of the case by 10 percent. How much would 3 cases of paintbrushes cost? How much would each brush cost?
5. Which is the better buy: 8 ounces of Brie cheese for $\$ 4.95$ or 12 ounces for $\$ 7.49$ ?

Debbie is a cook in a restaurant that is open 6 days a week. She is responsible for recording and monitoring the amount of money she spends on food. In the summer,
she uses an average of 9 loaves of bread per day.
a) On average, how many loaves of bread does Debbie use each week?

b) If bread costs $\$ 1.25$ per loaf to buy from a whores ale distributor, how much money should Debbie budget to purchase it, for the month of June? Assume that there are just 4 weeks in June.
7. The cost of a $355-\mathrm{mL}$ can of juice is $\$ 1.25$ in a vending machine. A $1.89-\mathrm{L}$ carton of the same juice costs $\$ 3.89$ at the grocery store. How much would you save per mL if you bought juice from the grocery store instead of the vending machine? (Hint: 1 L equals 1000 mL .)

8. Patricio is ordering cartons of detergent for resale in his store. He can order a carton of 12 for $\$ 34.68$ plus $\$ 5.45$ for delivery or a carton of 18 for $\$ 51.30$ plus $\$ 6.25$ for delivery. Which is a better buy, and by $\mathrm{h} \boldsymbol{\mathrm { w }}$ much per unit?


## Setting a Price

## REVIEW: WORKING WITH PERCENTS AND DECIMALS

percentage: a ratio with a denominator of 100; percent (\%) means "out of 100"

Dividing by 100
gives the same result as moving the decimal two places to the left. Many people use this as a shortcut.

In this section, you will calculate percentages and convert between percents and decimals.

Example 1
Comer $65 \%$ to a decimal.


To convert a percentage to a decimal, first convert it to a fraction with a denominator of 100, then divide the numerator by the denominator.
$65 \%$ means 65 out of 100 , or, stated as a fraction, $\frac{65}{100}$.
Divide 65 by 100 to express $65 \%$ as a decimal.
$65 \div 100=0.65$
$65 \%$ is equal to 0.65 .


## BUILD YOUR SKILLS

1. Convert the following percentages to decimals.
a) $78 \%$
b) $93 \%$
c) $125 \%$
<
d) $324 \%$
e) $0.5 \%$

g) $1.2 \%$
h) $100 \%$


## Example 2

Calculate $20 \%$ of 45 .

## SOLUTION

To find a percentage of a number, you can use proportional reasoning.
Let $x$ represent $20 \%$ of 45 . Use proportional reasoning to solve for $x$.


$$
\frac{20}{100}=\frac{x}{45}
$$

$$
4500\left(\frac{20}{100}\right)=\left(\frac{x}{45}\right) 4500 \quad \begin{aligned}
& \text { Multiply both sides of the equation by the } \\
& \text { product of the denominators. }
\end{aligned}
$$

$$
45 \times 20=100 x \quad \text { product } \quad \text { Simplify } .
$$

$$
\frac{900}{100}=\frac{100 x}{100} \quad \text { Divide both sides by } 100 \text { to isolate } x .
$$

$$
9=x
$$

$20 \%$ of 45 is 9 .

## alternative solution

First convert 20\% to a decimal.

$$
20 \div 100=0.20
$$

Then calculate $20 \%$ of 45 by multiplying 0.20 by 45 .

$$
\begin{aligned}
& x=0.20 \times 45 \\
& x=9
\end{aligned}
$$

## BUILD YOUR SKILLS

2. Calculate the following percentages.
a) $15 \%$ of 300

b) $45 \%$ of 1500

c) $140 \%$ of 70
e) $7.8 \%$ of 50
) $175 \%$ of 24
f) $0.3 \% \circ \circ 175$


## Example 3

What percent is 5 of 20 ?

## SOLUTION

To calculate what percent one number is of another means that you need to determine what number out of 100 is equivalent to your ratio.

You can use proportional reasoning to solve the question.

5 is $25 \%$ of 20 .
Multiply both sides of the equation by 100 .
Simplify.

ALTERNATIVE SOLUTION


5 of 20 is the same as $\frac{5}{20}$. You can find the percent by dividing 5 by 20.

$$
5 \div 20=0.25
$$

This is 25 hundredths, or $25 \%$.



## BUILD YOUR SKILLS

3. Calculate what percentage the first number is of the second (to the nearest tenth of a percent).
a) 65 of 325
b) $\mathbf{1 3 5}$ of 405

c) 68 of 42

e) 1 of 12


## NEW SKILLS: WORKING WITH MARKUPS AND TAXES

When a person owns a business, she usually buys merchandise at a wholesale price. Sne then sells it at a higher price, called a retail price, to make a profit. The retail price is often determined by adding a certain percentage of the wholesale price to the wholesale price. The amount added is referred to as the markup.

Sales taxes are usually added to the retail price. There are three kinds of taxes that you may need to consider when purchasing items: Goods and Services Tax (GST), Provincial
markup: the difference Watween the amount a deater sells a product
for (hetail arice) and the amount heor she paid for it (wholesale price) Sales Tax (PST), and Harmonized Sales Tax (HST).

For more information, see page 28 of MathWorks 10.

## Example 4

Melanie owns a clothing store. Her standard markup is $85 \%$. She bought a coat from the wholesaler at $\$ 125.00$.
a) What would the markup be?
b) How much would Melanie charge her customer for the coat?

SOLUTION
a) Change $85 \%$ to a decimal.
$N$
$85 \div 100=0.85$
Multyyy the wholesale price by the markup.

The markup i

b) Melanie would chargeher customer the wholesale price plus the markup.


With a markup of $85 \%$, Marnie wound charge her customer \$231.25.

## BUILD YOUR SKILLS

4. The markup on a bicycle in a sporting goods store is $185 \%$. The bicycle's wholesale price is $\$ 450.00$. What is the markup in dollars?

5. Marco buys a certain brand of shampoo from a supplier at $\$ 7.25$ per bottle. He sells it to his customers at a markup of $25 \%$. What would the markup be?

6. A hanbok is a formal, traditional outfit of Korean clothing. At a markup of $60 \%$, what would be the retail price for a child's hanbok with a wholesale price of $\$ 117.45$ ?

7. What should Max charge for a package of paper plates in his store if he bought them for $\$ 9.00$ and wants to make a $75 \%$ profit?

## Example 5

Quentin wants to buy a pair of steel-toed boots listed at $\$ 179.95$. How much will the boots cost if $5 \%$ GST and $6 \%$ PST are charged?

## SOLUTION

Calculate the GST by changing 5\% to a decimal and multiplying by the retail price.

$$
5 \div 100=0.05
$$

$$
0.05 \times \$ 179.95=\$ 9.00
$$

Calculate the PST by changing $6 \%$ to a decimal and multiplying by the retail price.

$0.06 \times \$ 179.85=\$ 10.80$
The final price is diculated by adding the tax amounts to the retail price.
$\$ 179.95+\$ 9.00+\$ 10.80=\$ 1.99 .75$
Quentin will have to pay $\$ 199.55$.

While it is
convenient for you to
use the methods in
Alternative Solutions
1 or 2 , the store
would have to use the first method because they must keep track of how much GST and PST they collect.

ALTERNATIVE SOLUTION 1

$$
5 \%+6 \%=11 \%
$$

$$
11 \div 100=0.11
$$

$0.11 \times \$ 179.95=\$ 19.79$

$$
\$ 179.95+\$ 19.79=\$ 199.74
$$

You can think about the retail price as $100 \%$ of the cost. If you add the two sales taxes ( $5 \%$ plus $6 \%$ equals $11 \%$ ) to this, the total cost is $111 \%$.

Convert $111 \%$ to a decimal and multiply this by the initial cost.

$$
\begin{aligned}
111 \div 100 & =1.11 \\
\$ 179.95 \times 1.11 & =\$ 199.74
\end{aligned}
$$

## BUILD YOUR SKILLS

8. What would you have to pay for a jacket that is listed at $\$ 99.95$ if you live in Nunavut, where the only tax is $5 \%$ GST?

9. Find the total cost of a washing machine that is being sold for $\$ 944.98$ in Saskatchewan, where PST is $6 \%$ and GST is $5 \%$.

10. Calculate the HST (12\%) on a return flight from Crarorook, BC to Vancouver, BC that costs $\$ 372.00$.

11. Saskatchewan charges 5\% GST and 6\% PST. How much GST and PST would Krista pay on a can of paint priced at $\$ 45.89$ ?
12. If the markup is $125 \%$ on a certain brand of jeans that have a wholesale price of $\$ 30.00$, what will the consumer pay, if GST and PST are each $5 \%$ ?

13. The max up on a restaurant meal is $250 \%$. A meal costs $\$ 7.25$ to produce. How much wilftre customer be charged, after markup and 5\% GST are applied?

## PRACTISE YOUR NEW SKILLS

1. Calculate the following percentages.
a) $5 \%$ of 72
b) $275 \%$ of 8
c) $\mathbf{1 5 2 \%}$ of 200
d) $6 \frac{3}{4} \%$ of 700
2. An electrician buys his material at the local hardware store, then charges his customer $20 \%$ more. The material for a given project is $\$ 253.75$ at the hardware store.
a) What is the markup?

b) How mud does he charge the customer for the material?

3. Maria is a florist in a small boutique Nf Maria paid her supplier $\$ 8.50 /$ doz for roses and sold them for $\$ 19.95$, what was the percent markup?

4. Garth buys snow tires from a dealer in Thunder Bay, ON. The tires cos $\$ 79,00$ each. To make a profit, he must mark them up $40 \%$. How much must a customer pay for 4 tires if there is a $12 \%$ HST on the final sale?
5. Because the cost of ingredients has gone up, Maurice has decided to increase the cost of meals in his restaurant by $12 \%$. How much will he now charge for a grilled salmon fillet that used to cost $\$ 17.95$ ?

6. The wholesale cost of a certain brand of T-shirts is $\$ 132.00 /$ dozen. To cover costs and make a profit Lorena marks them up by $75 \%$. If GST is $5 \%$ and PST is $7 \%$, what will a customer have to pay for 1 T-shirt?


7. An MP3 player that Harry wants to buy sells for $\$ 89.95$ in BC where there is $12 \%$ HST. When he is on holiday in Alberta (where there is only the $5 \%$ GST), Harry sees the same MP3 player for $\$ 94.89$. Which is a better buy and by hoy much?

## On Sale!

## NEW SKILLS: SALE PRICES

When you go shopping, you see signs that advertise promotions, such as "For Sale," "Up to $50 \%$ eff" and "Discounted Prices," that mean you will pay less than the price on the tag.

For more information, see page 34 of MathWorks 10.

## Example 1



Samantha wants to buy a new The model she likes costs $\$ 675.95$, but the clerk tells her that it is going on sale next week at $20 \%$ off. If Samantha waits one week, how much will she save on the price of the TYR

SOLUTION
The discount is $20 \%$, so find $20 \%$ of $\$ 675.95$ by multiplication.
Convert 20\% to a decimal.
$20 \div 100=0.20$

Multiply 0.20 by the original price.
$0.20 \times \$ 675.95=\$ 135.19$
The original price will be discounted by this amount, so Samantha would save \$135.19.

## BUILD YOUR SKILLS

1. How much will Jordon save on the price of a computer listed at $\$ 989.98$ if it is discounted by $30 \%$ ?
2. The Midtown Bakery sells Chinese specialties such as pineapple buns and lotus seed buns. Day-old goods at the bakery are sold at a discount of $60 \%$. If the original price of a loaf of stet bread was $\$ 2.98$, how much would you save by buying a day-old loaf?


3. If the sale price is $25 \%$ off, what will you save if you sofa regularly priced at \$999.97?


## Example 2

Michelle is a member of the Xat'sull First Nation and is fluent in the Shuswap language.
She works as a language instructor and gift shop cashier at the Xat'sull Heritage Village, near Williams Lake, BC.

The gift shop is selling off summer inventory. What will be the cost of a carving that was priced at $\$ 149.95$ if the sale sign says "Reduced by $60 \%$ "?


Calculate $60 \%$ of $\$ 4.95$ to determine the savings.
First, convert 60\% to decimal.
$60 \div 100=0.60$


Multiply the original price by 0.60
$0.60 \times \$ 149.95=\$ 89.97$
The original price will be reduced by this amount, so subtract $\$ 89.97$ from $\$ 149.95$.
$\$ 149.95-\$ 89.97=\$ 59.98$

The cost of the carving will be $\$ 59.98$.

## ALTERNATIVE SOLUTION

If the price of the carving is reduced by $60 \%$, that means that the customer will pay only $40 \%$ of the cost ( $100 \%$ minus $60 \%$ is $40 \%$ ).

Convert $40 \%$ to a decimal.
$40 \div 100=0.40$
Multiply the original price by 0.40 .
$0.40 \times \$ 149.95=\$ 59.98$
The carving will cost $\$ 59.98$.

## BUILD YOUR SKILLS

4. Sarbjit charges $\$ 24.95$ for a haircut in her beauty salon, but gives students a $30 \%$ reduction on Thursday evenings. How much would you have to pay to have your hair cut on a Thursday evening?
5. Margariet Manages a second-hand clothing store in Fin Flon, Manitoba. The store advertises that it you buy 3 items, you will get $15 \%$ off the most expensive item, $20 \%$ off the second most expensive, and $30 \%$ off the cheapest item. You choose three items costing $\$ 190, \$ 25.00$, and $\$ 12.00$. How much will you pay for the three items?

6. Normally Chiu charges $\$ 75.00$ to paint a room. However, if he paints 3 or more rooms for you, he gives you a $15 \%$ discount. How much will hedharge if he paints 4 rooms for you?


## Example 3

Lisa specializes in selling products from the Philippines, including rattan, bamboo, and palm baskets. Medium-sized bamboo baskets are regularly priced at $\$ 19.98$. They are on sale, advertised as "Buy one, get the second at half price." What is the discount rate, as a percent?


Calculate ne regular cost of 2 baskets.
$\$ 19.98 \times 2=\$ 39.96$
In buying 2 baskets, fou save half the price of 1 basket.
$\frac{1}{2}(\$ 19.99)=\$ 9.99$


Calculate the percent savings by dividing the discount by the regular price, and multiplying by 100 .
$\frac{\$ 9.99}{\$ 39.96} \times 100 \%=25 \%$
The discount rate is $25 \%$.


## BUILD YOUR SKILLS

7. What is the percentage markdown if a $\$ 175.00$ item sells for $\$ 150.00$ ?

8. In a store opening promotion, Fred advertises T-shirts: "Buy 4 get 1 free." If the cost of 1 T -shirt is $\$ 15.97$ what is the discount rate, as a percent?


9. Cameron is buying new computers for his office. Each computer costs $\$ 789.00$.

He is told that if he buys 5 computers, he can get a fth one free. What will be his percent saving compared to buying all 6 at the regular price?
10. Shelly works as an optician in Whitehorse, YT. Her store is selling last year's glasses frames at a savings of $30 \%$. What will you pay for frames that were originally priced at $\$ 149.00$ if $5 \%$ GST is charged?

GST and PST are
paid on the selling
price, not the original price.
11. Nicole wants to buy a coat originally priced at $\$ 249.95$. It is on sale at $25 \%$ off. How much will she pay if $5 \%$ GT and $5 \%$ PST are charged?

12. Yasmin owns a kitchen and bath fitting store. She is selling kitchen sink at a reduction of $40 \%$ because of a scratch in the finish. The originaprice was $\$ 249.95$.
a) Determine the total savings to the customer, including $5 \%$ GSKanda PST of $8 \%$.

b) Calculate the percentage of savings.

## PRACTISE YOUR NEW SKILLS

1. In Abbotsford, BC, Mack works as a used car salesman. He offers a $15 \%$ reduction to repeat customers. If the price marked on a car is $\$ 9879.00$, how much will it be reduced for a repeat customer?

2. A fishing rod originally priced at $\$ 49.98$ is reduced by $30 \%$.
a) How mach is the discount?

b) What will the cost be before tax?


3. Senior citizens are offered a $20 \%$ discount on their lunch on tuesdays in Hay River's local diner. How much will Rita and Dick, both senior citizens, se dee f hey order the teriyaki chicken salad at $\$ 14.98$ and the pork cutlets at $\$ 17.98$ ? (Ignore taxes.)
4. A can of paint costs $\$ 59.95$. There is a $20 \%$ price reduction for contractors. How much will the contractor save if he buys 5 cans?
5. A furnish/
a) How much wily y pay for a bedroom suite that originally cost $\$ 2989.97$ if GST is $5 \%$ and PST is 7

b) What are your total savings on this purchase
6. Robert sells bicycles, skateboards, and snowboards at his sporting goodstore

A bicycle that was originally priced at $\$ 785.00$ sold for $\$ 553.00$. What percent markdown did Robert offer?
7. The wholesale cost of a tawa, a griddle used to cook Indian flatbread, is $\$ 53.00$. A merchant marks it up $65 \%$. At the end of the season, he sells the remaining stock at $60 \%$ off.
a) What was his original asking price?

b) At the original price, how much would a customer pay with $5 \%$ GST and $5 \%$ PST?
c) What was th

d) How much would a customer pay when it was on sale, including 5\% GST and 5\% PST?



f) What would be the percentage savings?

## Currency Exchange Rates

## NEW SKILLS: EXCHANGE RATES

Different countries use different monetary units and/or different currencies. It is important when travelling to consider exchange rates, or the value of one monetary unit compared to another.
For more information, see page 41 of MathWorks 10.
exchange rate: the price
of one country's currency in terms of another country's currency

## Example 1

C
Lucas is a glazier who operates a window installation business. He regularly travels to the United States to buy supplies. Be fore travelling, he converts \$500.00 CAD into American dollars for personal expenses. Wee Canadian dollar is worth 0.94192 of an American dollar, how many Americandofars will Lucas receive in exchange for \$500.00 CAD?

## SOLUTION

Use unit pricing.

$$
\begin{aligned}
\$ 1.00 \mathrm{CAD} & =\$ 0.94192 \mathrm{USD} \\
\$ 500.00 \mathrm{CAD} & =\$ 0.94192 \mathrm{USD} \times 500 \\
\$ 500.00 \mathrm{CAD} & =\$ 470.96 \mathrm{USD}
\end{aligned}
$$

Lucas will receive \$470.96 USD.

## BUILD YOUR SKILLS

1. Ray purchased $\$ 500.00$ CAD worth of parts from Hungary for use in his garage. If the exchange rate is one Canadian dollar to 180.0779 Hungarian forints ( Ft ), how many forints will you receive for $\$ 500.00$ CAD?


C
2. If one Canadian dollars is worth 0.5911 British pounds sterling $(£)$, calculate how many pounds sterling you would get for $\$ 200.00$ CAD.


3. Madeline is attending a trade show in Denmark. She runs short of spending money and must convert $\$ 100.00$ CAD into Danish kroner (kr). The exchange rate is
5.3541 Danish krone for one Canadian dollar. How many kroner willshe receive?

## Example 2

One Thai baht is worth 0.023541 of a Canadian dollar. How many bahts would a tourist in Thailand receive for $\$ 200.00$ CAD?

SOLUTION

1. 00 baht $=\$ 0.023541 \mathrm{CAD}$
$200 \div 0.023541=8495.82$
For $\$ 200.00$ CAD, a tourist in Thailand would receive 8495.82 bahts.

## BUILD YOUR SKILLS

4. If the exchange rate for converting a Canadian dollar to the euro is 0.7180 on a particular day, how many euros wont you get for $\$ 300.00$ CAD?

5. The exchange rate for converting a Canadian dollar to the Swiss franc (SEr) is 1.0542. How many Swiss francs will you get for $\$ 400.00$
6. Canada imports steel, iron, and organic and inorganic chemicals from Trinidad and Tobago. The exchange rate for converting the Canadian to the Trinidad and Tobago dollar is 6.1805 . How many Trinidad and Tobago dollars will you get for $\$ 200.00$ CAD?
7. Using the following exchange rates, calculate how much foreign currency you would receive for $\$ 200.00$ CAD.
a) $\$ 1.00 \mathrm{CAD}$ is worth 1.72904 Brazilian reals

8. Calculate the value in Canadian dollars of an frem that costs $\$ 449.75$ Singapore dollars. Assume the exchange rate for one Canadian dollar is 0.75529 .

9. Henry returns home to Whale Cove, Nunavut, after a trip to Europe. On his travels he purchased a jacket for 125.98 euros. Calculate the value of Henry's jacket in Canadian dollars. Assume that a euro is worth 1.3987 of a Canadian dollar.

10. The exchange rate between the South African rand and the Canadian dollar is 0.138469 ( 1 rand equals $\$ 0.138469$ (AD). What is the cost in Canadian dollars of an item priced at 639.00 rand?


0/5

Exchanging money is not quite as simple as the transactions here show. Although the calculations will be the same, you have to consider bank buying rate and bank selling rate when exchanging currency. When the bank buys foreign currency from you, they pay you less than they charge

## Example 3

Anne works for an automotive parts distributor and visits Switzerland to source new products. On a given day, the bank selling rate of the Swiss franc compared to the Canadian dollar is 1.0501 and the buying rate is 1.0213 .
a) How many Swiss francs would Anne receive for $\$ 400.00$ CAD?
b) If Anne sold them back to the bank, how much would she receive?
c) What would her net loss be?

## sqution

a) Che bank will sell Swiss francs to Anne, so use the selling rate. 1 Swiss franc is wort 5.0501 CAD.

$\frac{1}{1.0501}=\frac{x}{400.00} \quad$ Omit the units.
$\begin{aligned}(400.00 \times 1.8501) \times \frac{1}{1.8501} & =\frac{x}{400.00} \times(1.0501 \times 400.00) \quad \begin{array}{l}\text { Multiply both sides of the equation } \\ \text { by the product of the denominators. } \\ \text { Simplify }\end{array} \\ 400.00 & =1.0501 x\end{aligned}$
$\frac{400.00}{1.0501}=x$
$380.92=x$
Anne would receive 380.92 Swiss francs.

## ALTERNATIVE SOLUTION

a) 1 Swiss franc is worth $\$ 1.0501$ CAD.
$\$ 1.00$ is therefore worth $\frac{1}{1.0501}$ Swiss francs. Multiply this by 400 to calculate
what $\$ 400.00 \mathrm{CAD}$ is worth. $400.00 \times \frac{1}{1.0501}=380.92$ Swiss francs
b) The bank buys the Swiss francs back at a rate of 1.0213 Swiss francs per \$1.00 CAD.

$$
\begin{aligned}
\frac{1 \mathrm{SFr}}{\$ 1.0213} & =\frac{380.92 \mathrm{SFr}}{x} \\
\frac{1}{1.0213} & =\frac{380.92}{x}
\end{aligned}
$$

Omit the units.
$(1.0213 \times x) \times \frac{1}{1.0213}=\frac{380.92}{x} \times(x \times 1.0213)$ Multiply both sides of the equation by the product of the denominators. Simplify.

Anne would receive $\$ 389.03$ CAD.

ALTERNATIVE SOLUTION
b) 1 Swiss franc is worth $\$ 1.0213$

Multiply 380.92 Swiss francs by 1.0213 to find the value in Canadian dollars.
$380.92 \times 1.0213=\$ 389.03 \mathrm{CAD}$

c) Anne's net loss would be $\$ 400.00$ minus what she received back.
$\$ 400.00-\$ 389.03=\$ 10.97$
Anne would lose $\$ 10.97$ in the transaction.

Unit rates often work best for exchanging currency.

When customers exchange money at a bank or other institution, the bank will usually only deal with paper money, not coins.

## BUILD YOUR SKILLS

11. If the exchange rate of a country compared to the Canadian dollar is 0.00519 , will you get more or less of their currency units when you exchange money?
12. Dianne works as a bank teller in Canmore, AB. A customer wishes to buy 250 British pounds at a rate of 1.5379 \$CAD. How many Canadian dollars would the British pound cost?

13. If the selling rate of a euro $(€)$ is 1.4768 and the buy lng rate is 1.4287 , how much would you lose if you exchanged $\$ 1000.00 \mathrm{CAD}$ for eros and then converted them back to \$CAD on the same day?

## PRACTISE YOUR NEW SKILLS

1. Using the following information, calculate how much of the foreign currency you would get for $\$ 500.00$ CAD. Round to the nearest unit.
a) $\$ 1.00$ is worth 95.4911 Japanese yen
b) $\$ 1.00$ is worth 1.41046 Turkish lira
c) $\$ 1.00$ is woth 0.680228 euro
d) $\$ 1.00$ is worth 6.43033 Chinese yuan

2. Damien is training to become a custontenservice representative at a credit union in Saskatoon, SK. Given the following exthange rates compared to the Canadian dollar, calculate how much foreign currency Danien would give to a customer who wished to convert $\$ 500.00$ CAD.
a) Mexican peso, 0.0818085
c) British pound, 1.3376
b) Estonian koon, 0.0939564

e) Indian rupee, 0.0229526
f) Russian ruble, 0.0352667
3. Using the rates from question \#1, calculate the amount you would get in Canadian dollars if you sold the following.
a) 8750 Japanese yen
b) 900 Turkish lira
c) 250 euro s
d) 3000 Chinese yuan
4. Use the exoflange rates from question \#2. Calculate how many Canadian dollars you would get for each of the following.
a) 6750 Mexican ness
b) 145 British pounds
c) 15000 Indian rupees

5. If the exchange rate is 0.1736 between the Norwegian krone and the Canadian dollar, what would the price be in Canadian dollars of an item hal cost 275 kroner?
6. A hand-woven shawl costs 35 Botswana pula. How much does it cost in Canadian dollars if the exchange rate is 0.1515 ?

7. If the selling race of the Omani rial is 2.96845 and the buying rate is 2.86145 , how much would you lose if you bought and then sold $\$ 800.00$ on the same day?



## CHAPTER TEST

1. When he works as a landscape gardener, Mark sometimes uses a powdered fertilizer. It must be mixed at a rate of 1 part of powder to 14 parts of water. How much water will Mark use for 3 litres of powder?
2. A carcass 5.5 litres of gas when it travels 100 km .
a)

b) How much fuel would be needed for 400 -km trip?


3. Loretta works as a surveyor near Burwash Landing, YT. Her map uses a scale of 2.5 cm : 100 km . On her map, two sites she must visit are 7.4 cm apart. Wat is the actual distance between the two sites?
4. If a package of 12 pens cost $\$ 38.98$, what is the cost of 1 pen?
$s$
5. If the wholesale price of 10 packages of smoked salmon is $\$ 99.50$, what will the cost be for one barge after a markup of $45 \%$ ?

6. The bakery in Lind, BC is selling day-old Buns at a $40 \%$ reduction. If the regular price is $\$ 4.79 / \mathrm{doz}$, what is the reduced price?


7. A sofa in a furniture store was originally $\$ 1899.00$. The price was "reduced $\boldsymbol{D}_{5}, 35 \%$ for quick sale." When it did not sell, the manager offered another reduction of 20
a) What was the final price of the sofa with $5 \%$ GST and $7 \%$ PST?

b) Is this the same as a $55 \%$ reduction? Show why or why not.
8. A furniture store in The Pas, Manitoba, advertises: "All weekend, no GST and no PST." If GST and PST are usually $5 \%$ each, what is the actual saving as a percent on an item that costs $\$ 24.97$ ?

C/
9. After primeplanting season was over, a horticulturist sold lilac bushes for $\$ 15.00$. If the original price jas $\$ 39.00$, what is the percentage markdown?


10. Non-profit agencies get a $12 \%$ reduction from Polly's Printers. How much will they save on a printing job that regularly costs $\$ 865.00$ ?
11. James works for an industrial lighting company. He travels to Hong Kong to attend a trade show. James sees a fluorescent track lighting unit priced at 1295.31 Hong Kong dollars. What is the cost in Canadian dollars if \$1.00 CAD is worth 7.3181 Hong Kong dollars?

12. Marian travels to Spain to visit her mother and father.
a) $\$ 1.00 \mathrm{CAD}$ is worth $€ 0.680228$. If Marian converts $\$ 450.00$ CAD into euros, how many euros does she receive?


b) During her visit, Marian buys a leather purse for $€ 125.00$. What is the cospin Canadian dollars?
